

# Optimization of Feed Chains and Large Reflectors

Peter Meincke, Michael Forum Palvig, Niels Vesterdal Larsen, and Erik Jørgensen  
TICRA  
Copenhagen, Denmark  
pme@ticra.com

**Abstract**—A higher-order Method of Moments formulation, accelerated with the Multi-Level Fast Multipole Method, and dedicated waveguide analysis methods constitute the foundation of efficient direct optimization of antenna systems consisting of feed chains and electrically large reflectors. A numerical example illustrates that the direct optimization approach gives better results than those obtained using traditional approaches, in which the reflectors and feed chains are optimized separately.

## I. INTRODUCTION

The RF optimization of large reflector antenna systems is typically performed using at least two separate software tools: One tool for the optimization of the reflector and another for the feed chain, consisting of waveguide components and feed horns. This multi-tool optimization approach is tedious and it also results in sub-optimal designs, since intermediate optimization goals must be introduced in the feed-chain, although these goals are not design goals of the combined feed-chain/reflector-antenna system. These metrics are merely introduced to decouple the feed chain optimization from that of the reflector. Typical intermediate goals are taper, phase centre, and cross polarization of the feed. The drawbacks of the multi-tool optimization approach are eliminated by using an integrated tool for which the entire antenna system, i.e. all reflectors, feeds, and waveguide components can be analyzed and optimized as a single model. However, for electrically large structures the typical calculation time for an accurate analysis is measured in minutes or hours and an optimization with many variables is thus infeasible.

In this paper, a fast and accurate hybridized analysis method, which is well suited for large scale optimization of the entire feed-chain/reflector system, is presented. The accuracy and speed of the method rely on: 1) State-of-the art analysis methods tailored for each component of the system and 2) a rigorous coupling between the components (hybridization). The Generalized Scattering Matrix (GSM) based hybridization scheme and some of the dedicated analysis methods will be introduced in Section II. In a numerical example in Section III it is shown that better performance is obtained when optimizing the feed chain in presence of the reflector in a single hybridized model.

## II. ANALYSIS METHODS

The ability to optimize a system relies on a fast forward analysis. Our goal is to optimize a full reflector system, including waveguide feed network, horn, and scattering of the reflector, but including all of this in a single full-wave

simulation is inefficient. Analyzing each component of the system with a dedicated method suitable for that type of component is much more efficient. It requires, however, that the analysis methods are rigorously coupled to each other. We have achieved this using a GSM description of the components, with separation at waveguide port interfaces. Some of the specific analysis methods are briefly introduced below.

### A. Mode Matching and Analytical Methods

Many waveguide components consist of straight waveguide sections with different dimensions, or they can be accurately modeled as such. The coupling from modes in one waveguide piece to the next can be found by Mode Matching, that is, imposing the continuity of the electric field at the interface of the two. Other waveguide junctions can be solved analytically, which is even more efficient than the Mode Matching.

### B. Higher-Order Method of Moments with MLFMM

The scattering matrices of waveguide devices of general shape may be found using the Method of Moments (MoM). The MoM is also essential for coupling the closed waveguide problem to open radiating antennas.

To reduce memory consumption, we employ the higher-order discretization scheme presented in [1]. The basis functions are modified Legendre polynomials of arbitrary order defined on curved quadrilateral patches. This scheme generally reduces the number of unknowns with a factor of 5 as compared to the popular RWG basis functions [2] on flat triangular patches, corresponding to a memory reduction of 25 times.

For exact coupling from the waveguide region to electrically large and huge structures such as the reflector surface, support structures and even a full satellite body, we use the Multi-Level Fast Multipole Method (MLFMM) implementation of [3], which is the first work to successfully combine the advantages of both higher-order basis functions and MLFMM.

## III. OPTIMIZATION EXAMPLE

The capability of the new approach is illustrated for an offset reflector system operating at 14.25 GHz with diameter  $D = 1$  m and focal length  $f = 0.6$  m (see Figure 1). The initial feed is an axially corrugated horn with extremely low cross polarization at the design frequency (more than 50 dB below peak).

The far-field patterns of the reflector system in the plane of maximum cross-pol are shown in Figure 3. Cross polarization

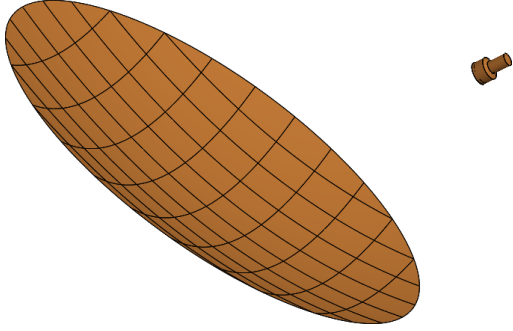


Fig. 1. The considered offset reflector configuration.  $D = 1$  m,  $f/D = 0.6$ .

lobes with the original feed (blue curve) are observed less than 20 dB below the peak of 42 dBi. This cross polarization is caused by the offset geometry, in spite of the near-perfectly polarized feed.

The cross polarization may be reduced by exciting specific modes in the horn [4]. The relevant mode for a circular horn is the  $TE_{21}$ . According to [4] the  $TE_{21}$  mode should be  $-20$  dB to  $-30$  dB below the fundamental mode and in phase quadrature with it.

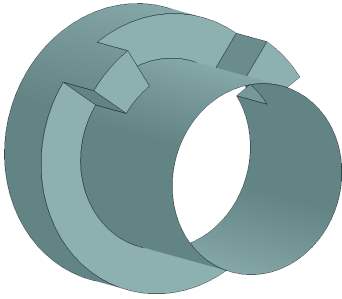


Fig. 2. The mode converter generating the higher-order  $TE_{21}$  mode.

A  $TE_{21}$  mode may be excited by an asymmetric waveguide mode converter. A mode converter of the type shown in Figure 2 is attached to the throat of the original horn.

If only the *multi-tool* approach were available, we would first optimize the horn and mode converter alone to the specifications given in [4]<sup>1</sup>. That is, the groove size and the length of the mode converter are optimized such that the  $TE_{21}$  mode content in the aperture of the horn is  $-20$  dB below and  $90^\circ$  behind the fundamental mode. Evaluating the secondary pattern with this modified feed, we get cross polarization shown as the orange curve in Figure 3. The peak cross polarization is reduced by 4.5 dB.

The improvement achieved above is moderate. We could amend the intermediate goals and do another iteration, but instead we perform a new optimization, in which the combined system is optimized directly. The mode converter, corrugated horn, and reflector are treated as a single model combining analytical methods, mode matching, and the HO-MoM/MLFMM

<sup>1</sup>In this work we use a gradient-based optimization approach.

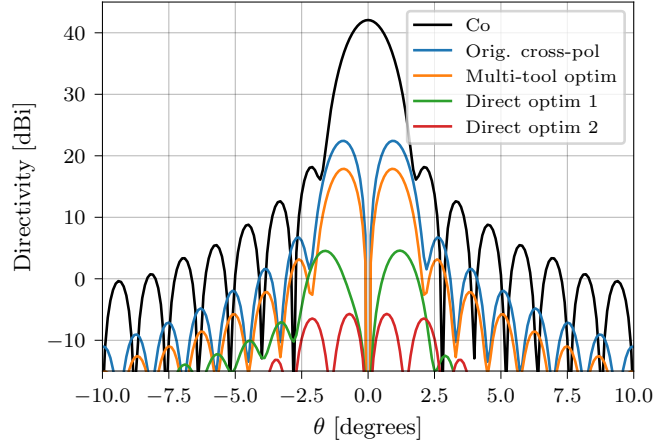


Fig. 3. The radiation pattern (in the plane of maximum cross) of the system after the three different feed optimizations. The *multi-tool* optimization imposes goals on the feed scattering parameters, while the *direct* optimizations impose goals directly on the far-field pattern. The co-polar pattern is virtually unchanged and thus plotted as one.

using the GSM-based hybridization. The optimized variables are still the mode launcher dimensions, but now the optimization goal is to directly minimize the far-field cross polarization level. The resulting cross polarization pattern is plotted as the green curve in Figure 3, showing an additional 13 dB of reduction compared to the *multi-tool* optimization. By including the depths of the 4 first corrugations in the optimization as well, the red curve in Figure 3 is obtained with an additional 10 dB improvement. Due to the highly efficient analysis method, each cost function evaluation takes only 3 seconds to calculate on a laptop computer.

#### IV. CONCLUSION

A rigorous hybridized approach based on several analysis methods combined with the generalized scattering matrix scheme is presented. It allows for fast and direct optimization of combined feed chains and reflectors with goals directly on the secondary radiation pattern. Through a numerical example it is illustrated that such direct optimization can give superior results compared the traditional approach in which feed chains and reflectors are optimized separately using two or more software tools.

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