# Brightness Temperature from Very Lossy Medium

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Abstract—The brightness temperature from moistured soil with a flat surface is computed by defining near-field bistatic transmission coefficients (BTCs) and modifying the Planck's law for lossy medium. The efficacy of the proposed methods are verified by simulations and comparison with literatures.

Keywords—brightness temperature, moistured soil, bistatic transmission coefficient, finite-difference time-domain method.

#### I. INTRODUCTION

In microwave passive remote sensing, the brightness temperature measured with radiometers is proportional to the specific intensity emitted from the ground [1]. In the Soil Moisture and Ocean Salinity (SMOS) mission, the brightness temperature was measured with an *L*-band interferometric radiometer to estimate the global soil moisture [2]. The Soil Moisture Active and Passive (SMAP) mission was conducted to collect information on global soil moisture, which significantly affects hydrology, meteorology and agriculture [3]. In microwave spectrum, the Rayleigh-Jeans approximation relates specific intensity to the physical temperature and surface emissivity [4].

Conventionally, bistatic transmission coefficients (BTCs) are the ratio of transmitted specific intensity above ground surface to the incident specific intensity just beneath ground surface [5]. Conventional BTCs and bistatic scattering coefficients (BSCs) are defined in terms of the far fields [1]. These coefficients work fine in lossless and low-loss media. In a lossy medium, the transmitted far fields approach zero, the BTCs thus defined will be zero.

In this work, near-field BTCs are defined in terms of variables right on the surface, and the boundary conditions on specific intensities can be expressed in terms of these near-field BTCs. The Planck's law is modified by differentiating group velocity and phase velocity. The finite-difference time-domain (FDTD) method is applied to compute near-field BTCs from a very lossy medium with flat surface. In conjunction with the modified Planck's law, the brightness temperatures are computed and compared with literatures.

## II. NEAR-FIELD BTCS

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Fig. 1. Scattering of fields from moistured soil in region (1) to air in region (0), via a flat surface.

Fig.1 shows a flat surface between a lossy moistured soil and air. The scattering of fields from region (1) to region (0) can be characterized by a near-field BTC as

$$\zeta_{pp'}^{01}(\hat{k}_{0u}^{2},k_{1u}) = \frac{K_{0up}(\hat{k}_{0u})}{K_{1up'}(\hat{k}_{1u})}$$

where  $K_{0up}(\hat{k}_{0u})$  (in unit Wm<sup>2</sup>) is called the transmitted power strength of *p*-polarization (p = h, v) in the direction  $\hat{k}_{0u}$ , which is defined in terms of the two-dimensional Fourier transforms of the equivalent electric surface currents  $\overline{J}_{e0u}$  and magnetic surface current  $\overline{M}_{e0u}$  on a Huygens' surface above the surface *S* between regions (0) and (1).

The conventional BTC from region (1) to region (0) is defined as  $\xi_{pp'}^{01}(\vec{k}_{0u}, k_{1u}) = \frac{4\pi r_0^2 I_{0up}(\hat{k}_{0u})}{P_{up'}(\hat{k}_{1u})},$ 

where  $I_{0up}(\vec{k}_{0u}) = \operatorname{Re}\{\overline{E}_{0up}(\overline{r_0}) \times \overline{H}_{0up}^*(\overline{r_0})\} \cdot k_{0u}/2$  is the farfield transmitted power density at  $\overline{r_0} = \hat{k}_{0u}r_0$ . If S is a flat surface, conventional and the near-field BTCs are related as  $\xi_{pp}^{01}(\vec{k}_{0u}, k_{1u}) = \frac{k_0^2 \cos \theta_{1u} A_g^2}{\pi X_b Y_b} \zeta_{pp}^{01}(\vec{k}_{0u}, k_{1u})$ , where  $A_g = L_x L_y$  is

the surface area in the computational domain.

### III. BOUNDARY CONDITION IN TERMS OF NEAR-FIELD BTCS

The boundary condition on *S* can be represented in terms of power strengths as

$$\frac{A_g \cos \theta_{0u}}{F_c r_0^2} K_{0up}(\hat{k}_{0u}) = \iint d\Omega_{1u} \frac{A_g}{X_b Y_b} \left[ \zeta_{pp}^{01}(\hat{k}_{0u}^2, k_{1u}) K_{1up}(\hat{k}_{1u}^2) + \zeta_{pp}^{01}(k_{0u}, \hat{k}_{1u}) K_{1up}(k_{1u}) \right]$$

which is reduced to the conventional boundary condition in terms of specific intensities as

$$\cos\theta_{0u}I_{0up}^{(0)}(\hat{k}_{0u}) = \frac{1}{4\pi}\iint d\Omega_{1u}\cos\theta_{1u}$$
$$\left[\xi_{pp}^{01}(\hat{k}_{0u}^{\prime}, k_{1u})I_{1up}^{(0)}(\hat{k}_{0u}^{\prime}) + \xi_{pp'}^{01}(k_{0u}, \hat{k}_{1u}^{\prime})I_{1up'}^{(0)}(k_{1u})\right]$$

The blackbody radiation intensity was originally derived in a lossless medium. The specific intensity is proportional to the energy density multiplied by the phase velocity. In a lossy medium, the specific intensity should be the energy density multiplied by the group velocity, namely,

$$I_{\nu} = \frac{\kappa T}{2\pi^2 \omega^2 \mu_0} \frac{k^{'3} (k^{'2} + k^{"2})}{\varepsilon_m k' + \varepsilon_m k''}$$

which is the modified Rayleigh-Jeans approximation. If region (1) is lossless and S is a flat surface, the boundary condition reduces to

$$\frac{T_{bp0}(\hat{k}_{0u})}{T_1} = \frac{1}{4\pi} \iint d\Omega_{1u} \left[ \xi_{pp}^{10}(-\hat{k}_{0u},-k_{1u}) + \xi_{pp}^{10}(-\hat{k}_{0u},-k_{1u}) \right]$$

which is the conventional formula to calculate the brightness temperature attributed to region (1).

#### IV. SIMULATIONS AND DISCUSSIONS

In the simulations, the near-field BTCs are computed by using the FDTD method with tapered incident fields. Fig.2 shows the brightness temperatures from a lossy medium with a flat surface. The frequency of incident field is  $f_c = 1.4$  GHz ( $\lambda = 21.43$  cm). The dielectric constant in region (1) is  $\varepsilon_{r1} = 17 - j2$ , leading to an effective conductivity of  $\sigma_1 =$ 0.1558 S/m and a skin depth of  $\delta_1 = 0.0341$  m. The effective wavelength in region (1) is about  $\lambda_1 = \lambda / \sqrt{\varepsilon_{r1}} = 0.24 \lambda$ . The spatial interval in the FDTD scheme is chosen as  $\Delta x = 0.05$  $\lambda_1 = 0.012 \lambda = 0.0026$  m. The surface size is chosen as  $L_x = L_y = 8\lambda$ .



Fig. 2. Brightness temperatures from a lossy medium of  $\varepsilon_r = 17 - j2$ , with a flat surface; solid curves: this approach, dashed curves: [6].

The errors of brightness temperatures are less than 1 K for  $\theta_0 < 40^\circ$  and around 5 K at  $\theta_0 = 50^\circ$ . The predictions with our approach agree reasonably well with those in [6].

#### V. CONCLUSION

In this work, a rigorous new approach is proposed to predict the brightness temperatures from a very lossy half space, by defining near-field BTCs and modifying the Planck's law. Simulation results with the FDTD method have verified the efficacy of this approach.

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